

# Automata Theory and Computability - 15CS54

## Module-5: Review Questions

| Sl. No.               | Questions  | Marks  |
|-----------------------|--|--------|
| <b>VARIANTS OF TM</b> |  |        |
| 1.                    | Explain the following types of TM:<br>a. Multitape TM<br>b. Non deterministic TM   | 6 each |
| 2.                    | Prove that every language accepted by a multi-tape TM is acceptable by some single-tape TM (that is, the standard TM).                               | 8      |
| 3.                    | Prove that, if $M_1$ is the single-tape TM that simulates multitape TM $M$ , then the time taken by $M_1$ to simulate $n$ moves of $M$ is $O(n^2)$ . | 6      |
| 4.                    | Prove that, if $M$ is a nondeterministic TM, there is a deterministic TM $M_1$ such that $T(M) = T(M_1)$   | 6      |
| 5.                    | Explain the model of Linear bounded Automata.  | 6      |

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| <b>DECIDABILITY</b> |   |        |
| 6.                  | Define :<br>a. recursively enumerable language<br>b. recursive language<br>c. decidable languages<br>d. undecidable languages   | 2 each |
| 7.                  | Prove that<br>a. $A_{DFA}$ is decidable.<br>b. $A_{CFG}$ is decidable.<br>c. $A_{CSG}$ is decidable.<br>d. $A_{TM}$ is undecidable.   | 6 each |
| 8.                  | Prove $HALT_{TM} = \{(M, w) \mid \text{The Turing machine } M \text{ halts on input } w\}$ is undecidable.  | 6      |
| 9.                  | a. Does the PCP with two lists $x = (b, bab^3, ba)$ and $v = (b^3, ba, a)$ have a solution?<br>b. Prove that PCP with two lists $x = (01, 1, 1)$ , $Y = (01^2, 10, 1^1)$ has no solution. | 2 each |
| 10.                 | If $L$ is a recursive language over $\Sigma$ , show that $\bar{L}$ ( $\bar{L}$ is defined as $\Sigma^* - L$ ) is also recursive.  | 4      |
| 11.                 | If $L$ and $\bar{L}$ are both recursively enumerable, show that $L$ and $\bar{L}$ are recursive.  | 6      |
| 12.                 | Show that the union of two recursively enumerable languages is recursively enumerable and the union of two recursive languages is recursive.  | 6      |

**COMPLEXITY AND COMPUTATION**

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| 13. | State and explain Church-Turing Thesis.  | 6 |
| 14. | Write a note on quantum computation.   | 8 |
| 15. | Let $f(n) = 4n^3 + 5n^2 + 7n + 3$ . Prove that $f(n) = O(n^3)$ .   | 4 |
| 16. | Find the running time for the Euclidean algorithm for evaluating $\gcd(a, b)$ where $a$ and $b$ are positive integers expressed in binary representation.      | 5 |
| 17. | Construct the time complexity $T(n)$ for the Turing machine $M : L = \{0^n 1^n : n \geq 1\}$   | 5 |
| 18. | Prove that, if $p(n) = a_k n^k + a_{k-1} n^{k-1} + \dots + a_1 n + a_0$ is a polynomial of degree $k$ over $\mathbb{Z}$ and $a_k > 0$ , then $p(n) = O(n^k)$ . | 6 |
| 19. | Prove that the growth rate of any exponential function is greater than that of any polynomial.   | 6 |